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The research question is: Does the data provide strong evidence that the mean blood pressure for those who exercise regularly is less than 75 mm Hg ?

- a) State the hypotheses (H_0 and H_a) to be tested.
 - b) Define the population parameter in (a)
 - c) Find the p-value for these data and state a conclusion at the $\alpha = .02$ level.
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- 1) Find the RR in terms of z-scores and test H_0 at the $\alpha = .02$ level.
 - 2) Write the RR for H_0 in terms of \bar{X}
 - 3) Find the probability of a Type II error if the true mean is 69 mm Hg .

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(a) $H_0: \mu = 75$ (b) μ represents the true mean bp for women who exercise regularly
 $H_A: \mu < 75$

(c) p-value = $P(\bar{X} \leq 70.7 | \mu = 75) = P\left(\frac{\bar{X} - \mu}{\sigma/\sqrt{n}} \leq \frac{70.7 - 75}{10/\sqrt{25}}\right)$
 $= P(Z \leq -2.15) = .0158$

(1) Reject H_0 if $z_s < -2.05$

(2) Reject H_0 if $\frac{\bar{X} - 75}{10/\sqrt{25}} < -2.05 \Rightarrow \bar{X} < 70.9$

(3) $\beta(69) = P(\text{Accept } H_0 | \mu = 69)$
 $= P(\bar{X} \geq 70.9 | \mu = 69)$
 $= P\left(\frac{\bar{X} - \mu}{\sigma/\sqrt{n}} \geq \frac{70.9 - 69}{10/\sqrt{25}}\right)$
 $= P(Z \geq .95) = 1 - .8289 = .1711$