

# CS 295A/395D: Artificial Intelligence

## Knowledge Representation

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The University of Vermont

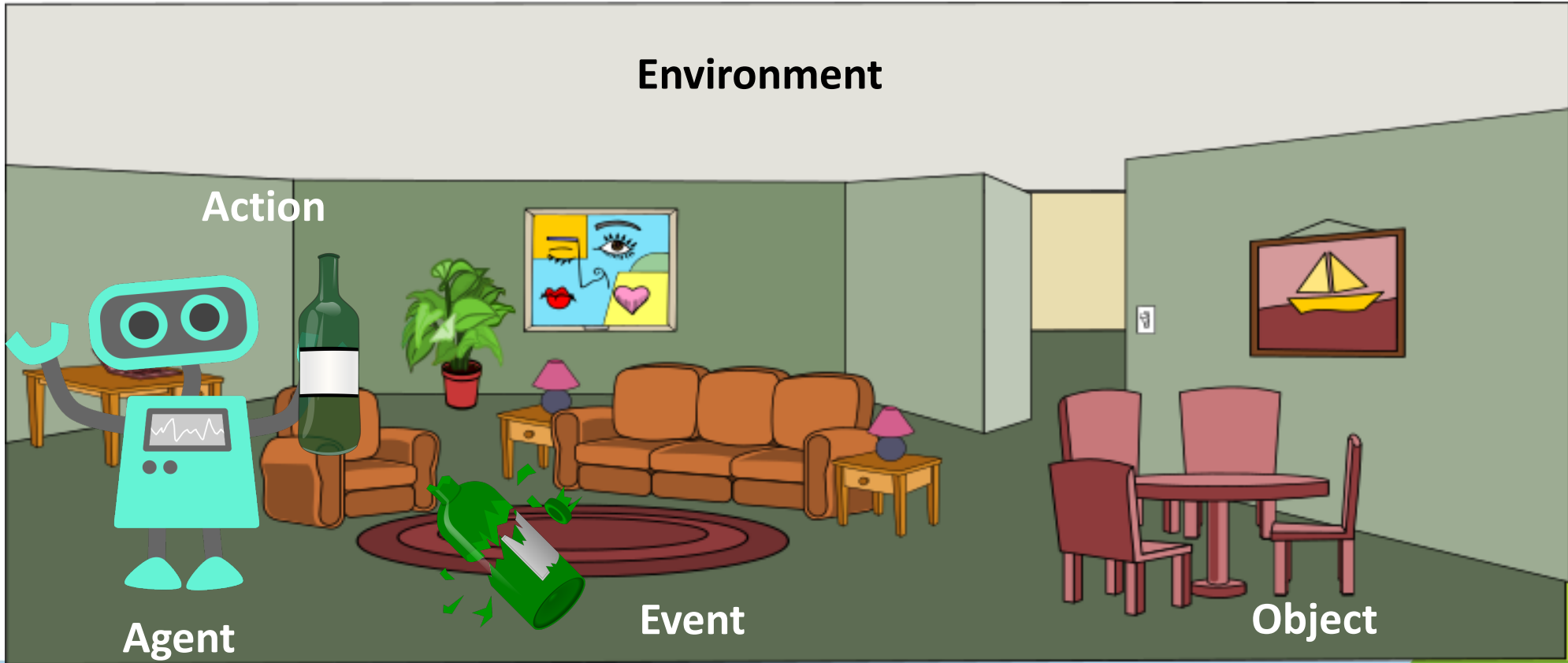
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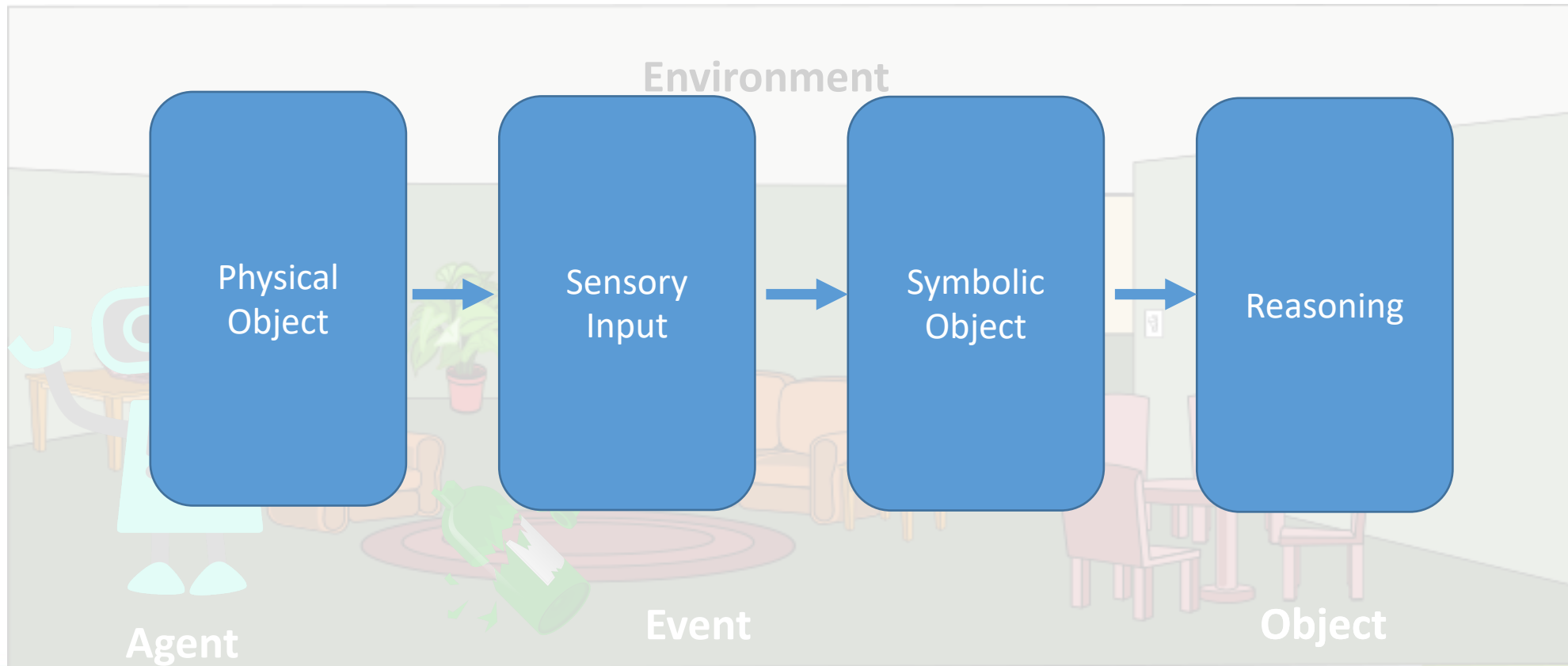
# Agenda

- **Knowledge Representation: Motivation**
- Ontologies: Categories and Relations
- Background Review: Set Theory Notation
- Clicker Questions
- *Bonus*: OOP as objects in an ontology

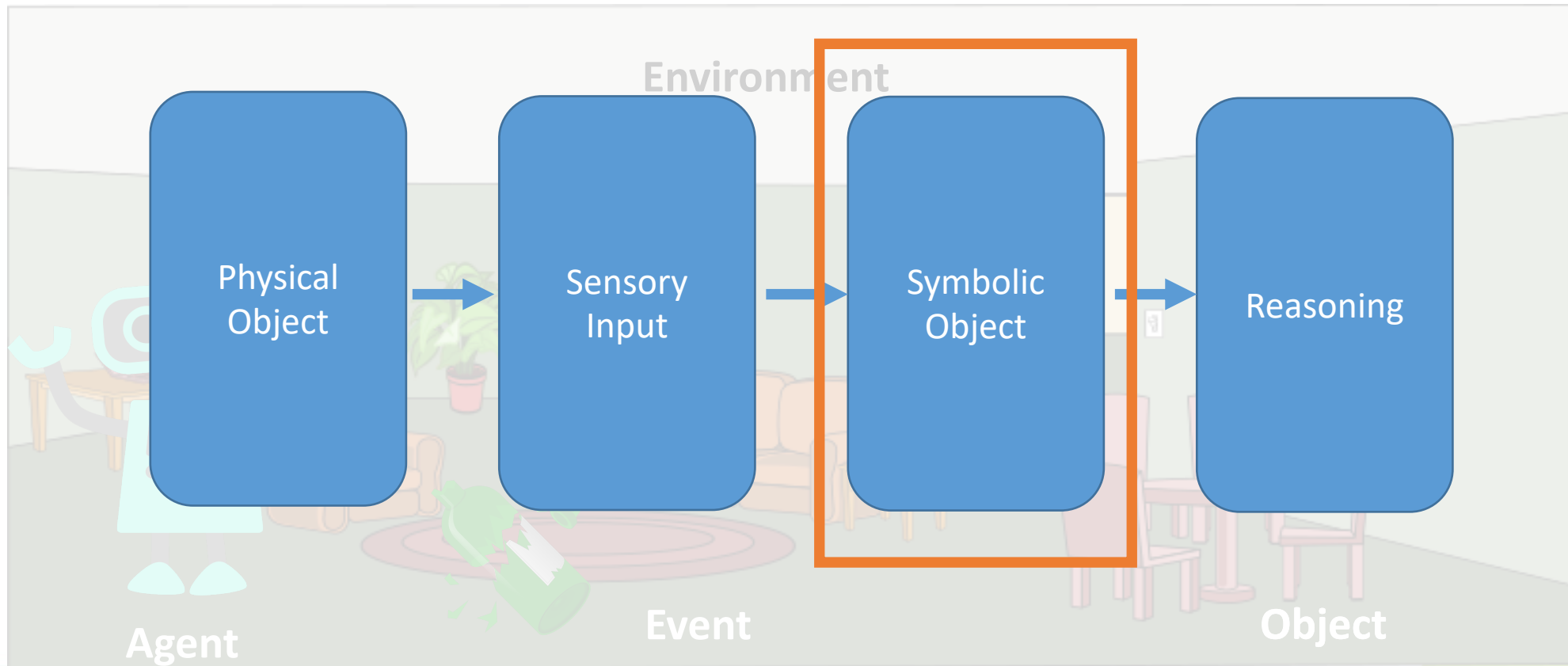
# Knowledge Representation: Motivation



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# Ontologies: Categories and relations

A **model** is a simplified representation of the behavior a system.

An **ontology** is a collection of **categories** and **relations**.

A category is a collection of **things/stuff** that share **relations**.

A **relation** is a pairing of instances from possibly different categories.

A model may use an ontology in its representation of a system's behavior.

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## Set Theory: Set definition and size

A set  $S$  is a container for a collection of objects called elements.

$$S = \left\{ \text{apple}, \text{orange}, \text{kiwi slice} \right\}$$

$|S|$  denotes the size of the set

$$|S| = \left| \left\{ \text{apple}, \text{orange}, \text{kiwi slice} \right\} \right| = 3$$

# Set Theory: Contains

$s \in S$  is an assertion saying that  $s$  is an element of  $S$ . (e.g.,  $\text{In}(s, S)$  or  $\text{ElementOf}(s, S)$ )

If  $S = \left\{ \text{apple}, \text{orange}, \text{kiwi} \right\}$ , then  $\text{apple} \in S$ .

If  $S = \left\{ \text{apple}, \text{orange}, \text{kiwi} \right\}$ , then  $\text{strawberry} \notin S$ .

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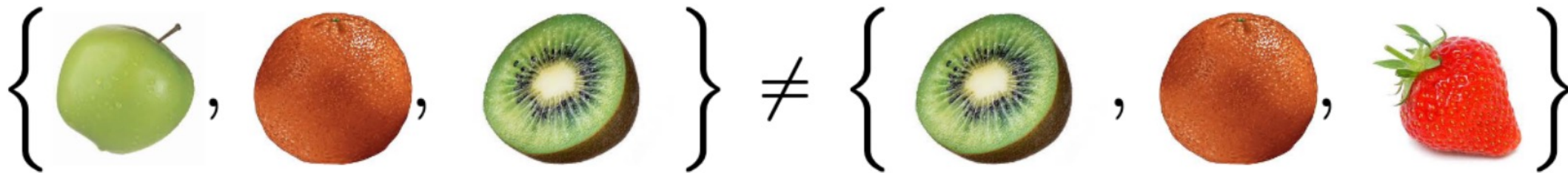
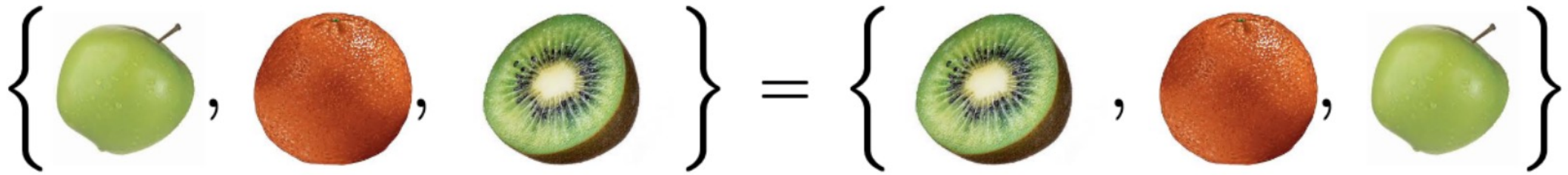
## Background: Classes of sets

- **Empty set:** The unique set that does not contain anything
- **Finite sets:** Contain a finite number of elements (e.g., fruit example)
- **Countably infinite sets:** Elements can be indexed by non-negative integers (e.g., even numbers, humans into the future)
- **Uncountably infinite sets:** Sets that cannot be indexed by the non-negative integers (e.g., real numbers between 0 and 1)

$$S = \{ \} = \emptyset$$

# Set Theory: Equality

$S = T$  is an assertion that  $S$  is equal to  $T$ . Two sets are equal iff every element of  $S$  is a member of  $T$ .



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$$\{\} \subseteq \left\{ \text{Kiwi slice}, \text{Orange}, \text{Apple} \right\}$$

## Set Theory: Subset

$T \subseteq S$  is an assertion that  $T$  is a subset of  $S$ .  $T$  is a subset of  $S$  iff every element of  $T$  is also an element of  $S$ .

$$\left\{ \text{Apple}, \text{Orange} \right\} \subseteq \left\{ \text{Kiwi slice}, \text{Orange}, \text{Apple} \right\}$$

$$\left\{ \text{Apple}, \text{Orange}, \text{Strawberry} \right\} \not\subseteq \left\{ \text{Kiwi slice}, \text{Orange}, \text{Apple} \right\}$$

## Set Theory: Subset

$T \subset S$  is an assertion that  $T$  is a strict subset of  $S$ .  $T$  is a subset of  $S$  iff every element of  $T$  is also an element of  $S$  and  $T \neq S$ .

$$\{ \text{apple}, \text{orange} \} \subset \{ \text{kiwi}, \text{orange}, \text{apple} \}$$

$$\{ \text{apple}, \text{orange}, \text{strawberry} \} \not\subset \{ \text{kiwi}, \text{orange}, \text{apple} \}$$

$$\{ \text{orange}, \text{kiwi} \} \not\subset \{ \text{kiwi}, \text{orange} \}$$



## Set Theory: Subset

$T \subset S$  is an assertion that  $T$  is a strict subset of  $S$ .  $T$  is a subset of  $S$  iff every element of  $T$  is also an element of  $S$  and  $T \neq S$ .

$$\{ \text{apple}, \text{orange} \} \subset \{ \text{kiwi}, \text{orange}, \text{apple} \}$$

$$\{ \text{apple}, \text{orange}, \text{strawberry} \} \not\subset \{ \text{kiwi}, \text{orange}, \text{apple} \}$$

$$\{ \text{orange}, \text{kiwi} \} \not\subset \{ \text{kiwi}, \text{orange} \}$$

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## Set Theory: Extensional vs. Intensional

Examples so far: *enumerated* set elements = *extensionally-defined*

Can also define sets in terms of their properties = *intensionally-defined*

- Even numbers are defined to be divisible by two
- Chairs are furniture that you can sit on



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## **Relationship between Ontologies and Sets**

Are categories sets?

Why or why not?

How would you decide?

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## Which of the following is *not* an ontology?

Feel free to ask clarifying questions about each of these

- A) Dewey Decimal System (library book categorization by topic)
- B) Binomial nomenclature (scientific name for living things)
- C) Computer Science major requirements
- D) Phylogenetic Trees

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# Concretizing Ontologies: Object-Oriented Programming

Write on board

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# Monday: Predicate Logic

Gluing it together before we break it apart...